



ADDITIONAL MATHEMATICS

0606/12

Paper 1

October/November 2016

MARK SCHEME

Maximum Mark: 80

Published

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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

Question	Answer	Marks	Part Marks
1 (a) (i)	10	B1	
(ii)	22	B1	
(iii)	4	B1	
(b) (i)	$Q \subset R$	B1	
(ii)	$P \cap Q = \emptyset$, or $\{ \}$	B1	
2	$a=1, b=-3, c=-1$	B3	B1 for each
3	$3y^2 + 5y - 2 = 0$ $y = \frac{1}{3}, y = -2$ $x = 3^{\frac{1}{3}}, x = 3^{-2}$ $x = 1.44, x = \frac{1}{9}$	B1, B1 M1 M1 A1, A1	B1 for $5y$ or $5\log_3 x$, B1 for -2 for correct attempt at the solution of <i>their</i> quadratic equation for dealing with one base 3 logarithm correctly A1 for each
4 (i)	$32x^{10} - \frac{80}{3}x^7 + \frac{80}{9}x^4$	B3	B1 for each term, powers of x must be simplified
(ii)	Coefficients needed: $\left(3 \times \textit{their} - \frac{80}{3}\right) + (1 \times \textit{their} 32)$ $= -48$	M1 A1	for dealing with 2 terms Allow A1 for $-48x^7$

Question	Answer	Marks	Part Marks
5 (i)	$\frac{dy}{dx} = \frac{3}{2(3x+2)}$	B1	for correct derivative of log function
	When $x = -\frac{1}{3}$, $y = 0$, $\frac{dy}{dx} = \frac{3}{2}$ Equation of normal: $y = -\frac{2}{3}\left(x + \frac{1}{3}\right)$	B1 M1 A1	for $y = 0$ M1 for attempt at a gradient of a perpendicular from differentiation and the equation of the normal
(ii)	$Q\left(0, -\frac{2}{9}\right)$ or $(0, 0.22)$ or better	B1 ft	Follow through on <i>their c</i> from part (i)
	$R\left(0, \frac{1}{2}\ln 2\right)$ or $(0, 0.35)$ or better	B1	
	Area of $PQR = \frac{1}{2}\left(\frac{1}{2}\ln 2 + \frac{2}{9}\right) \times \frac{1}{3}$ $= 0.0948$	B1	Allow 0.095
6 (a)	YX, XZ	B2	B2 for both with no extras B1 for 1 correct with or without extras B1 for both correct with extras B0 for anything else
(b) (i)	$\frac{1}{18}\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}$	B1, B1	B1 for $\frac{1}{18}$, B1 for $\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}$
	(ii) $\mathbf{C} = \mathbf{A}^{-1}\mathbf{B}$ $= \frac{1}{18}\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}\begin{pmatrix} -4 & 2 \\ 10 & 4 \end{pmatrix}$ $= \begin{pmatrix} -1 & 1 \\ 2 & 0 \end{pmatrix}$	M1 A1, A1	for pre-multiplication A1 for any correct pair of elements, but must be from correct matrices

Question	Answer	Marks	Part Marks
7	(i) $(0, \sqrt{3})$ or $(0, 1.73)$ or better	B1	B1 for each for correct attempt to solve trigonometric equation
	(ii) $\left(\frac{\pi}{6}, 2\right)$ or $(0.524, 2)$ or better	B1, B1	
	(iii) $\cos\left(x - \frac{\pi}{6}\right) = 0$ $x = \frac{2\pi}{3}$ oe or 2.09 or better	M1 A1	
	(iv) $2\sin\left(x - \frac{\pi}{6}\right)$ (+c)	B1	
	(v) Area = $\left[2\sin\left(x - \frac{\pi}{6}\right)\right]_0^{\frac{2\pi}{3}}$ = 2 + 1 = 3	M1 A1	
8	(i) $47 - 24 = 12\theta$ $\theta = \frac{23}{12}$, so $\theta = 1.917$ or better $\theta = 1.92$ to 2dp	M1 A1	for complete correct method to get $\theta =$ must have evidence of working to more than 2 dp, allow if 1.916 seen (truncated)
	(ii) $\sin\frac{\theta}{2} = \frac{CD/2}{12}$ $CD =$ awrt 19.6 or 19.7	M1 A1	for a complete method, may use cosine rule to get CD
	(iii) Area of sector = awrt 138 Area of triangle $AOB =$ awrt 67 or 68 Area of segment = awrt 70 or 71 $AD \times AB +$ segment area = 425 leading to $AD =$ awrt 18.1 or 18.0 Alternative method: Area of sector = awrt 138 Difference in length between BC (or AD) and OM where M is the midpoint of $CD = 6.88$, allow awrt 6.9 Remaining area consists of two trapezia each of width 9.85 and each of area 143.4 $\frac{1}{2}(2BC - 6.88) \times 9.85 = 143.4$ oe leading to $AD =$ awrt 18.1 or 18.0	B1 M1 M1 M1 A1 B1 M1 M1 M1 A1	for sector area, allow unsimplified for a correct attempt at area for segment area (<i>their</i> sector area – <i>their</i> triangle area) for complete method to find AD Allow A1 for 18 for sector area for attempt to find difference between parallel sides for area of one trapezium $\frac{1}{2}(2BC - \textit{their } 6.88) \times \textit{their } 9.85$ oe for attempt to find either BC or AD

Question	Answer	Marks	Part Marks
9 (i)	$p\left(\frac{3}{2}\right): \frac{27a}{8} - \left(4 \times \frac{9}{4}\right) + \frac{3b}{2} + 18 (=0)$	M1	for attempt at $p\left(\frac{3}{2}\right)$
	$p'\left(\frac{3}{2}\right) = \left(3a \times \frac{9}{4}\right) - \left(8 \times \frac{3}{2}\right) + b (=0)$	M1	for differentiation and attempt at $p'\left(\frac{3}{2}\right)$
	leading to $9a + 4b + 24 = 0$ oe and $27a + 4b - 48 = 0$ oe leading to $a = 4, b = -15$	M1 A1	for solution of simultaneous equations, to get either a or b for both
(ii)	$(x+2)(2x-3)^2$ oe	M1, A1	M1 for attempt at long division or factorisation
(iii)	$(x+2)(2x-3)^2 = x+2$ $x+2=0, x=-2$	B1	Must be using $(x+2)$ correctly using part (ii) to get $x=-2$
	$(2x-3)^2 = 1$ leading to $x=1, x=2$	M1 A1	for solution of the quadratic equation
10 (a) (i)	$20U + \frac{1}{2}\left(U + \frac{U}{2}\right)10 = 165$	M1	for realising that area under the graph is needed and attempt to find an area
	leading to $U = 6$	DM1 A1	for equating their area to 165 and attempt to solve
(ii)	Gradient of line: -0.3	M1, A1	M1 for use of the gradient, must be negative
(b) (i)	27	B1	
(ii)	$t^2 = 8 \ln 4$ $t = 3.33$ or better	M1 A1	for a correct attempt to solve $e^{\frac{t^2}{8}} = 4$
(iii)	acceleration = $3 \frac{2t}{8} e^{\frac{t^2}{8}} \left(e^{\frac{t^2}{8}} - 4 \right)^2$	M1, A1	M1 for a correct attempt to differentiate using the chain rule
	When $t = 1, a = 6.98$	M1, A1	M1 for use of $t = 1$ in their acceleration

Question	Answer	Marks	Part Marks
11 (i)	$\ln y = \ln A + x \ln b$ Gradient: $\ln b = -\frac{0.12}{8}, = -0.015$ $b = 0.985$ Intercept: $\ln A = 0.26$ $A = 1.30$	B1 M1 A1 DM1 A1	may be implied, if equation not seen specifically, by correct values for A and b for use of gradient to obtain $\ln b$ Allow A1 for $e^{-0.015}$ for use of one of the given points correctly Allow A1 for $e^{0.26}$ or 1.3
	Alternative 1 $\ln y = \ln A + x \ln b$ $0.2 = 4 \ln b + \ln A$ $0.08 = 12 \ln b + \ln A$ $A = 1.30$ and $b = 0.985$	B1 M1 DM1 A1, A1	for one correct equation for attempt to obtain either $\ln A$ or $\ln b$ from simultaneous equations Allow A1 for $b = e^{-0.015}$ and $a = e^{0.26}$ or 1.3
	Alternative 2 $1.22 = Ab^4$ $1.08 = Ab^{12}$ $A = 1.30$ and $b = 0.985$	B1 B1 M1 A1, A1	for correct attempt to obtain b or A , must already have B2 Allow A1 for $b = e^{-0.015}$ and $a = e^{0.26}$ or 1.3
(ii)	When $x = 6$, $\ln y = 0.17$ $y = 1.19$	M1 A1	for $\ln y = \text{their } \ln A + 6 \text{ their } \ln b$ or $y = \text{their } A \times (\text{their } b)^6$ allow awrt 1.18 to 1.20
(iii)	When $y = 1.1$, $\ln y = 0.095$ $x = 11$	M1 A1	for $\ln 1.1 = \text{their } \ln A + x \text{ their } \ln b$ or $1.1 = \text{their } A \times (\text{their } b)^x$ allow 10.5 to 11.5